

Supplemental Materials

Supplemental Material 1: Natural abundance correction

Definitions

m_0	The nominal mass of the compound ion, rounded to the nearest integer, with only the most abundant isotopes (e.g. ^1_1H , $^{12}_6\text{C}$, $^{14}_7\text{N}$)
m_i	The mass of the compound ion incremented by i above the nominal mass, due to incorporation of i isotopes with a higher mass than the most abundant (e.g. ^2_1H , $^{13}_6\text{C}$, $^{15}_7\text{N}$)
A_i	The recorded absolute intensity (peak area) in the mass spectrum of a compound ion at $m/z=m_i$
<i>Isotopologues</i>	Molecular species that have the same chemical formula, but differ in isotopic content and therefore in mass
<i>Tracer</i>	Here: stable-isotope labeled tracer, a compound in which one or more atoms have been replaced by a stable isotope, which allows the compound and its biochemical products to be distinguished from endogenous metabolites
ID	Isotopologue distribution, consisting of the fractional contributions of the masses of interest of the particular compound ion
\mathbf{K}	The representation of the <i>measured</i> ID as a vector
\mathbf{M}	The representation of the ID as a vector, <i>after correction</i> for natural abundance of isotopes
K_i	Element of the vector \mathbf{K} representing the <i>measured</i> fractional abundance of the isotopologue with mass m_i

M_i	Element of the vector \mathbf{M} representing the fractional abundance of the isotopologue with mass m_i <i>after correction</i> of K_i for the contribution of naturally occurring isotopes
\mathbf{L}	The correction matrix that converts the measured fractional abundance vector \mathbf{K} into the corrected matrix \mathbf{M}
L_j^i	Element L_j^i of the correction matrix \mathbf{L} , denoting the probability that an isotopologue in which i atoms were substituted for their corresponding stable isotope from the tracer, is heavier by an additional j mass units due to incorporation of naturally occurring isotopes.

General procedure

An isotopologue of mass m_i has a mass increment i above the nominal mass of the compound. The mass increment can originate from the tracer or from naturally occurring isotopes. A correction is necessary to transform the measured isotopologue distribution (ID) into the distribution that should have been observed had there been no naturally occurring isotopes. The method described here is based on the *measured* ID of the unlabeled, baseline sample that was obtained prior to addition of the stable isotope labeled tracer. What is new, at least to our knowledge, is the use of this *measured* ID of the baseline sample to reconstruct the skewed correction matrix \mathbf{L} (1; 2). We developed this method for compounds with a low fractional enrichment (typically less than 5%) in combination with a high molecular mass, such as metabolites that have been derivatized for GC-MS measurements. In these cases the generally accepted deviation of the enrichment of the baseline sample after correction ($\pm 0.4\%$), based on the default error for GC-MS measurements (3), would be substantial relative to the enrichment due to label incorporation. The general part of the procedure works as follows.

The vector \mathbf{K} is the measured ID, defined as:

$$\mathbf{K} = \begin{bmatrix} K_0 \\ K_1 \\ K_2 \\ \dots \\ K_n \end{bmatrix}$$

in which n is the number of atoms that can be substituted with a heavy isotope, and:

$$K_i = A_i / \sum_{i=0}^n A_i$$

Analogously a vector \mathbf{M} of corrected fractional abundances is defined as:

$$\mathbf{M} = \begin{bmatrix} M_0 \\ M_1 \\ M_2 \\ \dots \\ M_n \end{bmatrix}$$

in which element M_i represents the fractional abundance of the isotopologue with mass m_i after correction for natural isotope abundance, i.e. the fractional abundance that can be attributed to the tracer. \mathbf{M} is calculated from \mathbf{K} according to:

$$\mathbf{K} = \mathbf{L} \cdot \mathbf{M}$$

in which

$$\mathbf{L} = \begin{bmatrix} L_0^0 & 0 & 0 & \dots & 0 \\ L_1^0 & L_0^1 & 0 & \dots & 0 \\ L_2^0 & L_1^1 & L_0^2 & \dots & 0 \\ \dots & \dots & \dots & \dots & 0 \\ L_n^0 & L_{n-1}^1 & L_{n-2}^2 & \dots & L_0^n \end{bmatrix}$$

The elements L_j^i of the correction matrix \mathbf{L} denote the probability that an isotopologue in which i atoms were incorporated from the stable-isotope labeled substrate, is heavier by an additional j mass units due incorporation of naturally occurring isotopes.

The elements of the first column of \mathbf{L} (L_j^0) denote the probabilities that measured isotopologues are exclusively labeled by naturally occurring isotopes, as would be the case in the baseline sample prior to addition of the tracer. When one atom has been replaced by a heavy isotope from the tracer, the number of atoms of the compound that can be substituted with a naturally occurring isotope is $n-1$. If i atoms are

substituted by isotopes originating from the labeled substrate, then the other $n-i$ atoms have a probability of being labeled by naturally occurring isotopes. Since this probability depends on the number of the other $n-i$ unlabeled atoms, the \mathbf{L} matrix becomes ‘skewed’ (1; 2), i.e. the columns are not just shifted relative to each other, but the probabilities differ, i.e. $L_j^i \neq L_j^{i+1}$.

If matrix \mathbf{L} is known, vector \mathbf{M} is calculated as follows.

Given: $\mathbf{K} = \mathbf{L} \cdot \mathbf{M}$. Then: $\mathbf{L}^{-1} \cdot \mathbf{K} = \mathbf{L}^{-1} \cdot \mathbf{L} \cdot \mathbf{M}$ and thus: $\mathbf{L}^{-1} \cdot \mathbf{K} = \mathbf{M}$. Hence, to solve \mathbf{M} , matrix \mathbf{L} is inverted and the resulting matrix \mathbf{L}^{-1} multiplied to vector \mathbf{K} .

Most often, matrix \mathbf{L} is calculated from the known abundances of naturally occurring isotopes (4). In cases with a high enrichment with isotopes from the tracer, this approach is sufficiently accurate. It may become problematic for large molecules with a low isotope enrichment from the tracer. In these cases the generally accepted deviation of the enrichment of the baseline sample after correction ($\pm 0.4\%$) would be substantial relative to the enrichment due to label incorporation. Then, the baseline sample provides an independent measurement of the actual ID due to naturally occurring isotopes. There are, however, no measured IDs of the compound with i tracer isotopes atoms incorporated, due to a lack of such standards. This implies that there is only information for the first column of \mathbf{L} . Below, we derive a method to construct the skewed \mathbf{L} matrix, based on the measured baseline sample.

Constructing the \mathbf{L} matrix from the measured baseline samples

To compute the skewed \mathbf{L} matrix from the measured ID of the baseline sample, we were inspired by (5), who derived the ID (vector \mathbf{K}) for a molecule composed of two chemical fragments X and Y with mutually independent isotopologue distributions. The isotopologue distribution (K_0, K_1, K_2, \dots) of a molecule consisting of a fragments X with isotopologue distribution (p_0, p_1, p_2, \dots) and a fragment Y with isotopologue distribution (q_0, q_1, q_2, \dots) can be computed according to:

$$\begin{bmatrix} p_0 & 0 & 0 & \dots & \dots \\ p_1 & p_0 & 0 & \dots & \dots \\ p_2 & p_1 & p_0 & \dots & \dots \\ p_3 & p_2 & p_1 & \dots & \dots \\ \dots & \dots & \dots & \dots & \dots \\ p_n & p_{n-1} & p_{n-2} & \dots & \dots \end{bmatrix} \cdot \begin{bmatrix} q_0 \\ q_1 \\ q_2 \\ \dots \\ \dots \end{bmatrix} = \begin{bmatrix} K_0 \\ K_1 \\ K_2 \\ \dots \\ \dots \end{bmatrix}$$

Note that here we do not have a skewed matrix: the columns containing $p_0 - p_n$ are just shifted relative to each other, as the equation describes different combinations of the same fragments. We used the same principle here. The measured isotopologue was considered to consist of two parts i.e. T^{i*} and R^i . Part T^{i*} , the ‘tracer part of the compound’, accounts for the incorporated isotopes from the tracer, while part R^i , the ‘rest of the molecule’, accounts for the incorporation of naturally occurring isotopes of all atoms in the rest of the molecule. This tracer part T^{i*} is not a chemical fragment of the molecule, but just the total of the heavy elements from the tracer. The asterisk denotes that this is the labeled version of T^i , since we will later distinguish it from the equivalent part of the molecule T^i without the tracer isotopes incorporated. The natural isotopologue distribution vector \mathbf{R}^i of the fragment R^i can be written as:

$$\mathbf{R}^{-i} = \begin{bmatrix} R_0^{-i} \\ R_1^{-i} \\ R_2^{-i} \\ \dots \\ R_{n-i}^{-i} \end{bmatrix}$$

in which element R_j^{-i} denotes the probability that part R^i lacking i labeled atoms, has a mass increment of j due to incorporation of naturally occurring isotopes. The correction matrix \mathbf{L} can now be constructed according to:

$$\mathbf{L} = \begin{bmatrix} R_0^0 & 0 & 0 & \dots & 0 \\ R_1^0 & R_0^{-1} & 0 & \dots & 0 \\ R_2^0 & R_1^{-1} & R_0^{-2} & \dots & 0 \\ \dots & \dots & \dots & \dots & 0 \\ R_n^0 & R_{n-1}^{-1} & R_{n-2}^{-2} & \dots & R_0^{-n} \end{bmatrix}$$

The first column \mathbf{R}^0 ($i = 0$) is the isotopologue distribution of the unlabeled baseline sample prior to addition of the tracer (vector \mathbf{K}^0). The key question is how to identify the isotopologue distributions \mathbf{R}^i for $i \neq 0$.

To obtain \mathbf{R}^{-i} we have to start with the ID of the baseline sample. The ID of the unlabeled compound in a part T^i (the unlabeled equivalent of T^*) and a part R^{-i} . Suppose that we have a compound $X_k Y_l Z_m$ with n atoms X that can be substituted for a stable isotope from the tracer. The compound can be perceived to consist of a part T^i , equivalent to X_i , and a remainder R^{-i} , equivalent to $X_{k-i} Y_l Z_m$, with $i \in [1 - n]$. The probability s_j^i that T^i contains j heavy atoms due to natural abundance, is calculated according to:

$$s_j^i = \frac{i!}{j! \cdot (i-j)!} \cdot (t_0)^{i-j} \cdot (t_1)^j$$

in which t_1 is the known fractional natural abundance of the stable isotope of atom X and $t_0 = 1 - t_1$. Since the isotopologue distributions of T^i and R^{-i} are mutually independent, according to Lee (5) we can write:

$$\underbrace{\begin{bmatrix} s_0^i & 0 & 0 & \dots & 0 & \dots \\ s_1^i & s_0^i & 0 & \dots & 0 & \dots \\ s_2^i & s_1^i & s_0^i & \dots & 0 & \dots \\ \dots & \dots & \dots & \dots & 0 & \dots \\ s_i^i & s_{i-1}^i & s_{i-2}^i & \dots & s_0^i \end{bmatrix}}_{T^i} \cdot \underbrace{\begin{bmatrix} R_0^{-i} \\ R_1^{-i} \\ R_2^{-i} \\ \dots \\ R_{n-i}^{-i} \end{bmatrix}}_{R^{-i}} = \underbrace{\begin{bmatrix} K_0^0 \\ K_1^0 \\ K_2^0 \\ \dots \\ K_n^0 \end{bmatrix}}_{K^0}$$

in which vector \mathbf{K}^0 denotes the measured ID of the baseline sample. Thus, for the unlabeled sample we can dissect the measured isotopologue vector \mathbf{K}^0 into:

$$\mathbf{T}^i \cdot \mathbf{R}^{-i} = \mathbf{K}^0$$

Therefore: $[\mathbf{T}^i]^{-1} \cdot \mathbf{T}^i \cdot \mathbf{R}^{-i} = [\mathbf{T}^i]^{-1} \cdot \mathbf{K}^0$ and thus: $\mathbf{R}^{-i} = [\mathbf{T}^i]^{-1} \cdot \mathbf{K}^0$. Hence, to solve \mathbf{R}^{-i} , matrix \mathbf{T}^i is inverted and multiplied to vector \mathbf{K}^0 .

This calculation is repeated n times, each time with a new matrix \mathbf{T}^i to calculate \mathbf{R}^{-i} for each i . In this way n vectors \mathbf{R}^{-i} with elements R_j^{-i} are calculated. The vectors \mathbf{K}^0 and \mathbf{R}^{-i} are then inserted as columns to form the \mathbf{L} matrix with $L_j^0 = K_j^0$ and $L_j^i = R_j^{-i}$.

In the current study a deuterium label has been used and the intensity of isotopologues with masses $m_0 - m_4$ have been measured. Therefore, $X = {}^1_1H$ and $n = 4$, so $i \in [0 - 4]$. The fractional natural abundance of 2_1H

has been reported to be 0.0115 % (6), thus $t_I = 0.000115$. In the accompanying Excel sheet (Supplemental File 1) the calculations are done for [6,6- $^2\text{H}_2$]-glucose measured by GC-MS as the penta-acetate derivative.

Finally, why is this method more appropriate for samples with a very low label enrichment in large molecules? If we derive the L matrix from natural isotope abundances (the state-of-the art method), for a large molecule small errors in individual isotope abundances may accumulate to a relatively large error. In the here described method, the natural abundances are used only to compute the ID of the small part T^i and thus the cumulative error is much smaller. We checked that in our dataset the state-of-the-art method gave rise to deviations of less than 0.4% in the baseline sample, indicating that the quality of the measurements was good.

Supplemental Material 2: Analytical solutions of simple tracer model

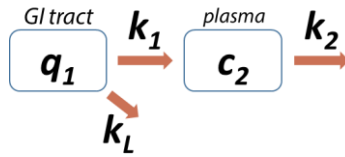


Figure A1: Two-compartment model of tracer kinetics

To derive general characteristics of the tracer kinetics, the compartment model depicted in Figure A1 was solved analytically. q_1 and c_2 represent the amount and concentration of the tracer in compartment 1 and 2 respectively. In the case of an oral gavage, q_1 represents a gastrointestinal compartment ($\mu\text{mol} \cdot \text{kg}^{-1}$) and c_2 the plasma compartment (mM). Rate constant k_L refers to the loss of tracer before it reaches the plasma compartment.

The system is described by the following set of ordinary differential equations (ODE, cf. Research Design and Methods section for a motivation of the model equations):

$$\frac{dq_1}{dt} = -(k_1 + k_L) \cdot q_1 \quad (\text{Eq. S2.1})$$

$$\frac{dc_2}{dt} = \frac{k_1 \cdot q_1}{Vol} - k_2 \cdot c_2 \quad (\text{Eq. S2.2})$$

In matrix notation, this is equivalent to:

$$\frac{d}{dt} \begin{bmatrix} q_1 \\ c_2 \end{bmatrix} = \begin{bmatrix} -(k_1 + k_L) & 0 \\ +k_1/Vol & -k_2 \end{bmatrix} \cdot \begin{bmatrix} q_1 \\ c_2 \end{bmatrix} \quad (\text{Eq. S2.3})$$

which can be written as:

$$\dot{\mathbf{x}} = \mathbf{A} \cdot \mathbf{x} \quad (\text{Eq. S2.4})$$

This has the general solution:

$$\mathbf{x} = s_1 \cdot e^{\lambda_1 t} \cdot \mathbf{u}_1 + s_2 \cdot e^{\lambda_2 t} \cdot \mathbf{u}_2 \quad (\text{Eq. S2.5})$$

in which λ_1 and λ_2 are the eigenvalues of matrix \mathbf{A} , and \mathbf{u}_1 and \mathbf{u}_2 the corresponding eigenvectors.

The eigenvalues of \mathbf{A} are calculated from:

$$\det(\mathbf{A} - \lambda \mathbf{I}) = 0 \quad (\text{Eq. S2.6})$$

and:

$$(\mathbf{A} - \lambda \mathbf{I}) \cdot \mathbf{u} = \mathbf{0} \quad (\text{Eq. S2.7})$$

This yields eigenvalues $\lambda_1 = -(k_1 + k_L)$ and $\lambda_2 = -k_2$ with eigenvectors:

$$\mathbf{u}_1 = \begin{bmatrix} 1 \\ \frac{k_1}{Vol \cdot (k_2 - k_1 - k_L)} \end{bmatrix} \text{ and } \mathbf{u}_2 = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \quad (\text{Eq. S2.8})$$

This leads to:

$$q_1 = s_1 \cdot e^{-(k_1 + k_L)t} \quad (\text{Eq. S2.9})$$

$$c_2 = \frac{s_1}{Vol} \cdot \frac{k_1}{k_2 - k_1 - k_L} \cdot e^{-(k_1 + k_L)t} + s_2 \cdot e^{-k_2 t} \quad (\text{Eq. S2.10})$$

With:

$q_1(0) = q_{1,0}$ and $c_2(0) = 0$, the solution becomes:

$$q_1 = q_{1,0} \cdot e^{-(k_1 + k_L)t} \quad (\text{Eq. S2.11})$$

$$c_2 = \frac{q_{1,0}}{Vol} \cdot \frac{k_1}{k_2 - k_1 - k_L} \cdot e^{-(k_1 + k_L)t} - \frac{q_{1,0}}{Vol} \cdot \frac{k_1}{k_2 - k_1 - k_L} \cdot e^{-k_2 t} \quad (\text{Eq. S2.12})$$

In pharmacokinetics, the bioavailability of the tracer, *i.e.* the fraction that reaches the plasma compartment, is computed as the ratio between the area under the c_2 curve for an oral versus an intravenous administration.

For the oral administration as solved above, the area under the curve for c_2 becomes:

$$\begin{aligned} AUC_{oral} &= \int_0^{\infty} c_2(t) dt = \frac{q_{1,0}}{Vol} \cdot \frac{k_1}{k_2 - k_1 - k_L} \int_0^{\infty} (e^{-(k_1+k_L)t} - e^{-k_2 t}) dt \\ &= \left(\frac{q_{1,0}}{Vol \cdot k_2} \right) \cdot \frac{k_1}{k_1 + k_L} \quad (\text{Eq. S2.13}) \end{aligned}$$

Had the same amount of tracer been administered intravenously (IV), *i.e.* directly into the plasma compartment, the kinetics would be described by:

$$\frac{dc_2}{dt} = -k_2 \cdot c_2 \quad (\text{Eq. S2.14})$$

with:

$$c_2(0) = \frac{q_{1,0}}{Vol} \quad (\text{Eq. S2.15})$$

which leads to:

$$c_2 = \frac{q_{1,0}}{Vol} \cdot e^{-k_2 t} \quad (\text{Eq. S2.16})$$

Now the area under the curve becomes:

$$AUC_{IV} = \int_0^{\infty} c_2(t) dt = \frac{q_{1,0}}{Vol} \int_0^{\infty} e^{-k_2 t} dt = \frac{q_{1,0}}{Vol \cdot k_2} \quad (\text{Eq. S2.17})$$

And thus:

$$F = \frac{AUC_{oral}}{AUC_{IV}} = \frac{k_1}{k_1 + k_L} \quad (\text{Eq. S2.18})$$

This is a logical outcome, since it corresponds to the fraction of q_I that is transported to compartment 2.

Based on the analytical solution above, equation S2.12 describing the tracer kinetics can be simplified to:

$$c_2(t) = C \cdot (e^{-k_2 t} - e^{-k_a t}) \quad (\text{Eq. S2.19})$$

in which:

$$k_a = k_1 + k_L \quad (\text{Eq. S2.20})$$

and thus:

$$k_1 = k_a \cdot F \quad (\text{Eq. S2.21})$$

$$C = -\frac{q_1(0)}{Vol} \cdot \frac{k_1}{k_2 - k_1 - k_L} = -\frac{q_1(0)}{Vol} \cdot \frac{k_a \cdot F}{k_2 - k_a} \quad (\text{Eq. S2.22})$$

Thus, if C , k_a and k_2 are fitted from the data, the apparent distribution volume Vol can be calculated from the bioavailability F or *vice versa*. We are aware that we have derived here only classical pharmacokinetics equations, but it clarified (1) that the k_a fitted to tracer kinetics is only an apparent absorption rate constant, while the actual rate constant k_1 equals $k_a \cdot F$, and (2) what is the basis for the calculation of the apparent volume Vol from F . The latter is used to express the endogenous glucose production (EGP) in $\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{kg}^{-1}$.

Supplemental Material 3: Data fitting and identifiability

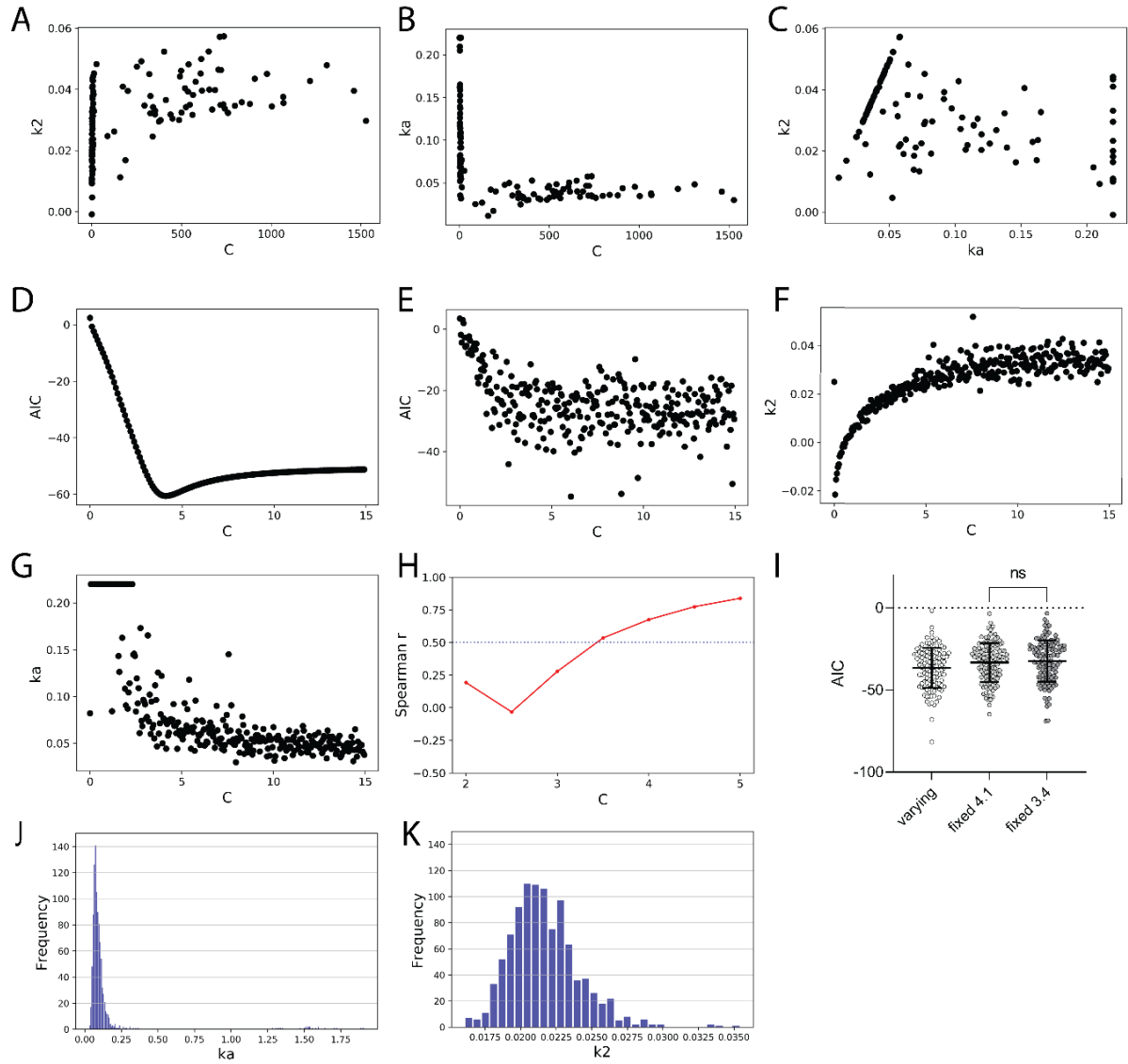


Figure A2: Correlations between all 3 parameters obtained from the tracer fit for all animals, with k_a with an upper bound of 0.22 (A, B, C). AIC values (D) derived from fitting of data values for a fixed C ranging from 0 and 15 for the mean values per time point. AIC (E), k_2 (F) and k_a (G) values derived in which a random variation was included in the mean values according to the distribution of the original dataset (H). Spearman correlation coefficient r between k_a and k_2 for model fit with different fixed values for C . Data were randomly generated according to mean and distribution for all time points (H). AIC comparison for model fits with the use of data from all animals. C was let to vary or was fixed at 4.1 or 3.4 (I). Expected distribution for k_a (J) and k_2 (K) from 1,000 fits based on the distribution of data randomly generated according to mean and distribution for all time points.

To obtain C , k_a and k_2 , the time course of tracer data for each animal (mM) was fitted to equation 11 $[q_2(t) = C \cdot (e^{-k_2 t} - e^{-k_a t})]$. Not all three parameters were identifiable from the tracer data due to collinearity (Fig. A2A-C). Given the intrinsic biological information contained in k_a and k_2 , C was selected to be fixed at 3.4 for the fits, based on (i) the lowest AIC (Akaike's Information Criterion for model selection) for data mean per time point (Fig. A2D, E), and on (ii) a Spearman correlation coefficient between k_a and k_2 lower than 0.5, based on 1 000 simulations of synthetic data (Fig. A2H). These assumptions did not interfere with the obtained AIC for the data fit (Fig. A2I). The constant k_a was constrained within the 95% CI of the median ($0.047 - 0.22 \text{ min}^{-1}$) to avoid biologically inconsistent outliers, based on the expected distribution from synthetic data (Fig. A2J, K). The constant k_2 was not constrained. Within the region of C values resulting in low AIC, k_a and k_2 did not heavily depend on the choice of C (Fig. A2F, G).

The lack of correlation between k_a and k_2 (Fig A3A) implies that both could be independently identified. The use of a more complex model including an extra distribution compartment and consequently a second elimination term did not result in better fits of the data and impaired identification of the elimination constant(s) (Fig. A3B, C). This is in agreement with analysis of human OGTT data, in which even more time points were taken due to the larger blood volume, and yet one elimination compartment was sufficient to fit the data accurately (7).

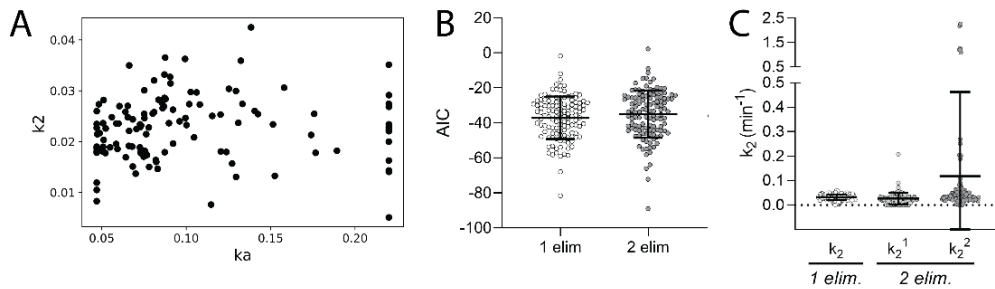


Figure A3: Scatter plot for k_a and k_2 values for fits with fixed C at 3.4 and applied boundaries for k_a (A). Comparison for all animals in the dataset when fitting tracer data using either 1 elimination term $[q_2(t) = C \cdot (e^{-k_2 t} - e^{-k_a t})]$ or 2 elimination terms $[q_2(t) = C_1 \cdot e^{-k_2^1 t} + C_2 \cdot e^{-k_2^2 t} - (C_1 + C_2) \cdot e^{-k_a t}]$ for AIC (B) and for elimination constants (C). A second elimination constant did not improve the AIC. Moreover, the second elimination constant could not be estimated, as is obvious from the large spread in the fitted values.

Supplemental figures

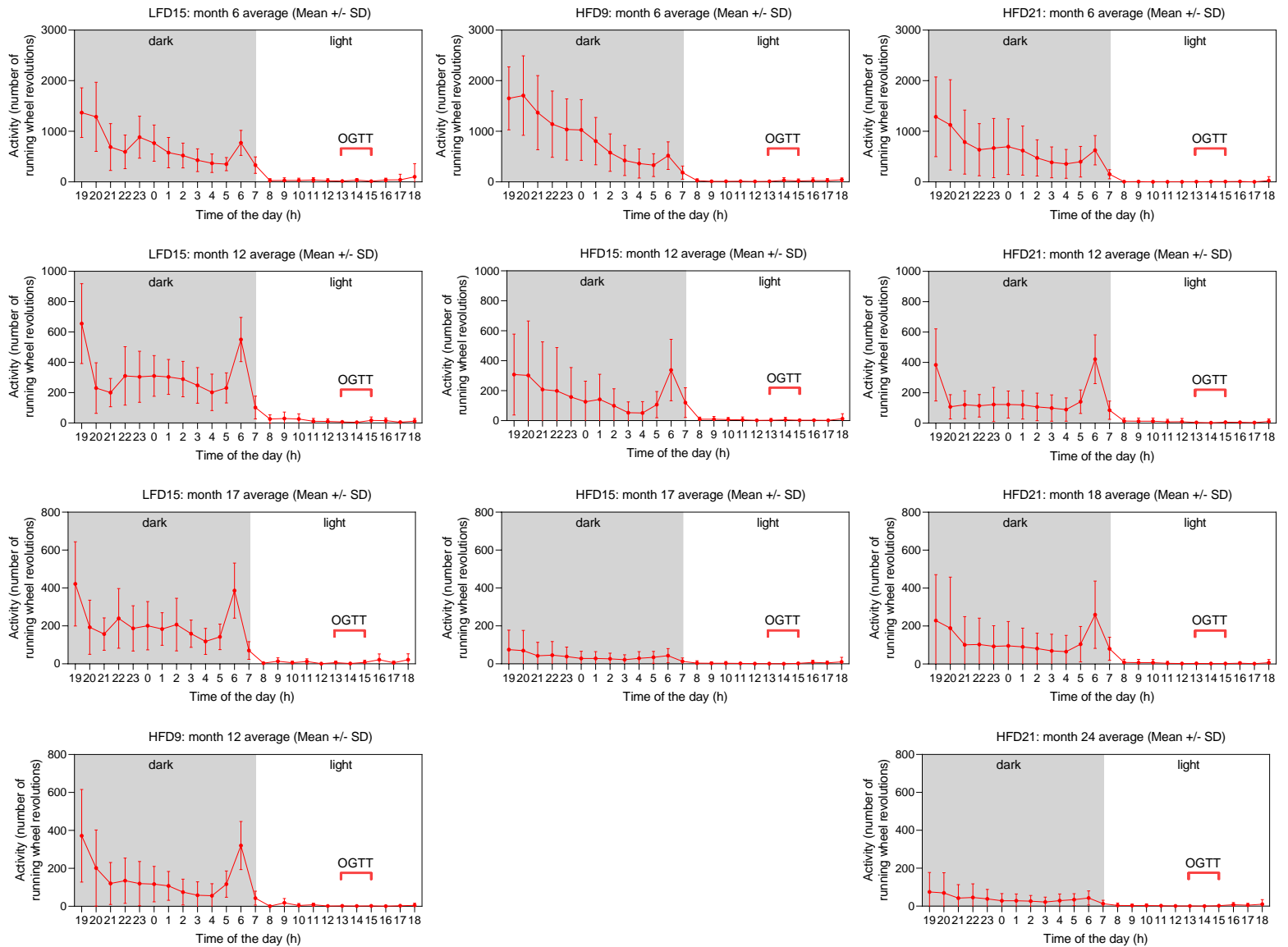


Figure S1: Average of running wheel activity in number of revolutions per hour. Data represent the average of all animals per experimental group on a given month (specified per panel). The diet group (LFD or HFD) is directly followed by a number, which indicates the experimental age group, as indicated in the materials and methods section. Dark and light phases are indicated, as well as the period of time in which the OGTT was conducted. Data are shown as mean \pm SD, n = 16-26.

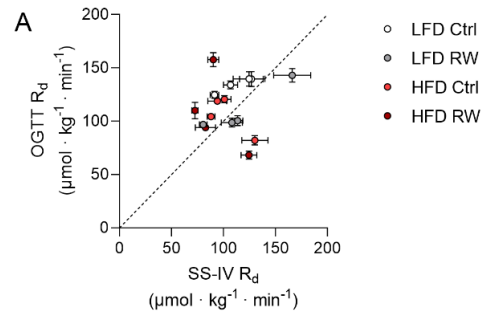


Figure S2: Comparison of the rate of glucose disposal (R_d) at basal state between the tracer OGTT and steady-state intravenous infusion (IV-SS) data, age matched. The dashed line represents the identity line ($y=x$). Scatter plot of data plotted as mean \pm SEM, $n = 6-8$.

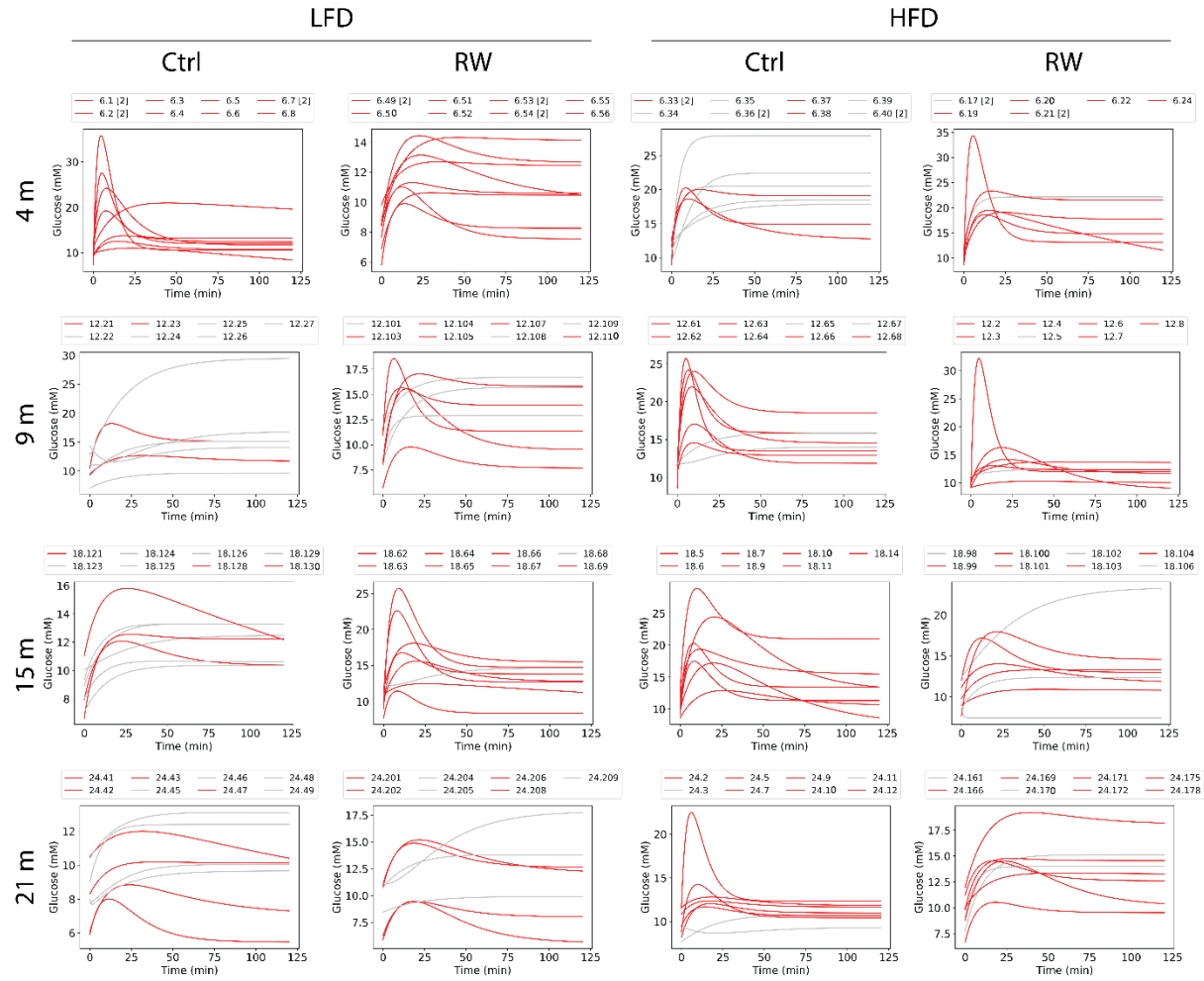


Figure S3: Individual fits for unlabeled glucose curves. Above each graph the mouse IDs are shown. Curves that showed an absorption followed by a clearance phase (red) were used for the EGP calculation. Curves in gray did not show the expected behavior and therefore were not included in the dataset to compute the EGP. This was done due to the high uncertainty in the obtained phenomenological constants for the unlabeled glucose in the absence of a clearance phase. In total, 37 animals were excluded, which were distributed among different groups.

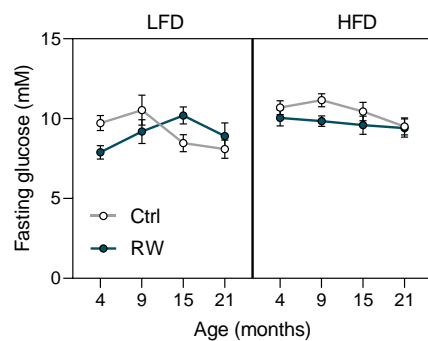


Figure S4: Fasting glucose values for each group. Data are shown as mean \pm SEM, $n = 6-8$.

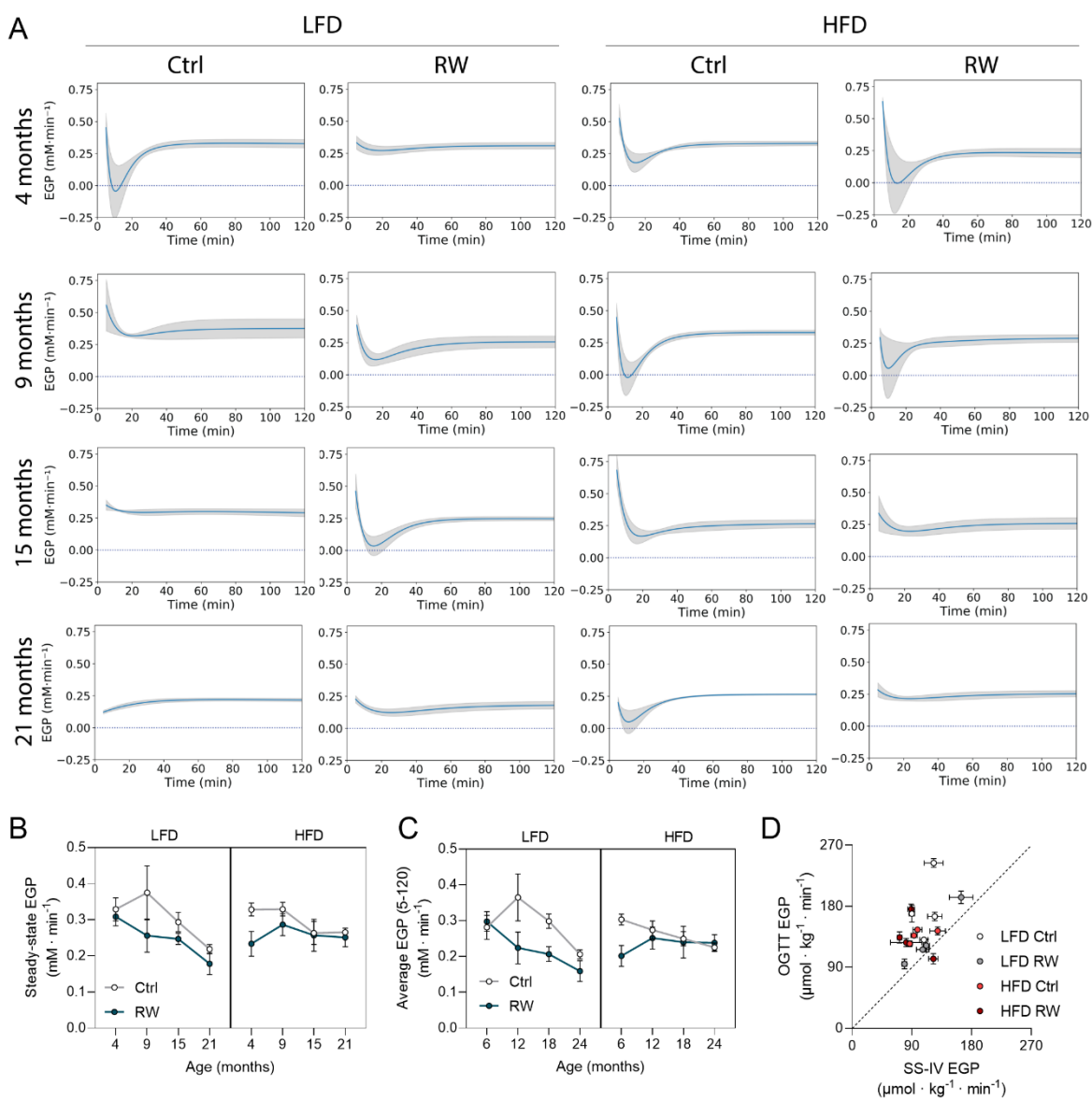


Figure S5: EGP* time courses in $\text{mM} \cdot \text{min}^{-1}$ (A). Each column represents a different diet and activity group, whereas each row represents a different age. LFD: low-fat diet, HFD: high-fat high-sucrose diet, Ctrl: sedentary mice, RW: mice submitted to voluntary running wheel. Mean EGP (line) \pm SEM (shaded area) is shown per experimental group. Steady-state EGP* values in $\text{mM} \cdot \text{min}^{-1}$ (B) calculated from the curves (mean \pm SEM). Average EGP* values in $\text{mM} \cdot \text{min}^{-1}$ (C) obtained from OGTT timeframe (5-120 min). Comparison of the steady-state EGP at basal state between the tracer OGTT and SS-IV datasets, age matched (D). The dashed line represents the identity line ($y=x$). Scatter plot of data plotted as mean \pm SEM, $n = 2-8$.

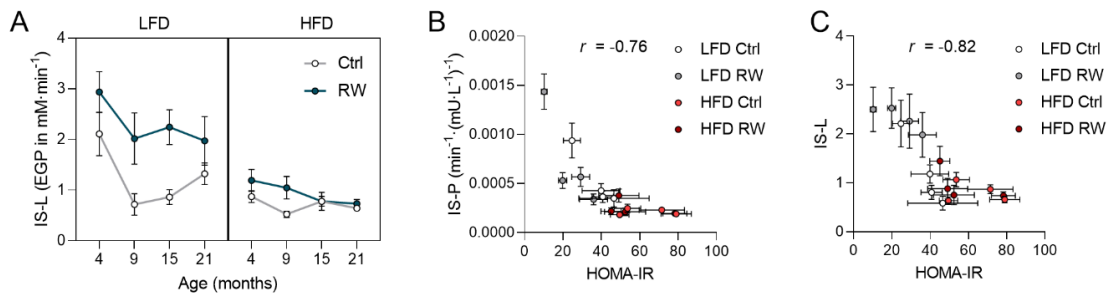


Figure S6: IS-L calculated from EGP in $\text{mM} \cdot \text{min}^{-1}$ (average from 5-120 minutes was used) (A). Data are shown as mean \pm SEM, $n = 2-8$. Correlations between HOMA-IR and IS-P (B) or IS-L (C), Pearson correlation coefficients (r) are shown. Scatter plot of data plotted as mean \pm SEM, $n = 2-8$.

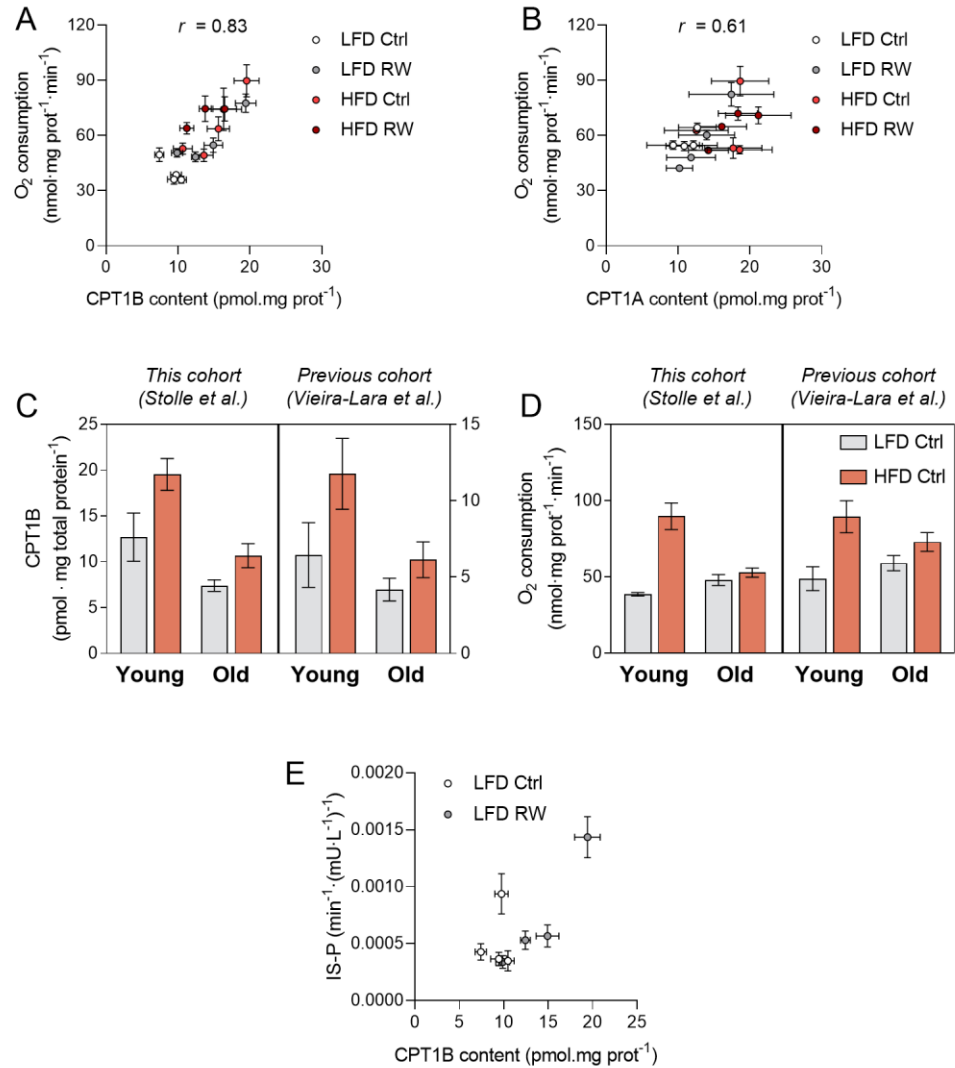


Figure S7: Correlation between CPT1B and oxidative capacity in the skeletal muscle, with the use of palmitoyl-CoA, carnitine and malate as substrates (A). Correlation between CPT1A and oxidative capacity in the liver, with the use of palmitoyl-CoA, carnitine and malate as substrates (B). Comparison between CPT1B levels (C) and oxidative capacity (palmitoyl-CoA, carnitine and malate as substrates) (D) in the skeletal muscle of mice from this present cohort (data from Stolle et al., 2018 (8), young = 4 months, old = 21 months, C57BL/6JOLA^{Hsd} background) and from a previous cohort (data from (9), young = 6 months, old = 21 months, C57BL/6J background). Correlation between CPT1B content and IS-P for LFD groups (E). Data are plotted as mean \pm SEM, $n = 4-8$.

References

1. Midani FS, Wynn ML, Schnell S: The importance of accurately correcting for the natural abundance of stable isotopes. *Anal Biochem* 2017;520:27-43
2. Dietze J, van Pijkeren A, Egger AS, Ziegler M, Kwiatkowski M, Heiland I: Natural isotope correction improves analysis of protein modification dynamics. *Anal Bioanal Chem* 2021;413:7333-7340
3. Antoniewicz MR: A guide to ^{13}C metabolic flux analysis for the cancer biologist. *Experimental & Molecular Medicine* 2018;50:1-13
4. Su X, Lu W, Rabinowitz JD: Metabolite Spectral Accuracy on Orbitraps. *Anal Chem* 2017;89:5940-5948
5. Lee WN, Byerley LO, Bergner EA, Edmond J: Mass isotopomer analysis: theoretical and practical considerations. *Biol Mass Spectrom* 1991;20:451-458
6. Audi G, Wapstra AH: The 1993 update to the atomic mass evaluation. *Nuclear Physics A* 1995;595:409-480
7. Cobelli C, Dalla Man C, Toffolo G, Basu R, Vella A, Rizza R: The oral minimal model method. *Diabetes* 2014;63:1203-1213
8. Stolle S, Ciapaite J, Reijne AC, Talarovicova A, Wolters JC, Aguirre-Gamboa R, van der Vlies P, de Lange K, Neerincx PB, van der Vries G, Deelen P, Swertz MA, Li Y, Bischoff R, Permentier HP, Horvatovitch PL, Groen AK, van Dijk G, Reijngoud DJ, Bakker BM: Running-wheel activity delays mitochondrial respiratory flux decline in aging mouse muscle via a post-transcriptional mechanism. *Aging Cell* 2018;17:1-11
9. Vieira-Lara MA, Dommerholt MB, Zhang W, Blankestijn M, Wolters JC, Abegaz F, Gerding A, van der Veen YT, Thomas R, van Os RP, Reijngoud DJ, Jonker JW, Kruit JK, Bakker BM: Age-related susceptibility to insulin resistance arises from a combination of CPT1B decline and lipid overload. *BMC Biol* 2021;19:154